Pearson Edexcel
Level 1/Level 2 GCSE (9 - 1)

Centre Number

Candidate Number

Mathematics AO3
Mathematical problem solving
Gold Test 3

Grades 6-9

Time: 60 minutes

Paper Reference
1MA1

You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser.

Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided
  – *there may be more space than you need*.
- **Calculators must not be used in questions marked with an asterisk (*).**
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must **show all your working out** with your **answer clearly identified** at the **end of your solution**.

Information

- This gold test is aimed at students targeting grades 6-9.
- This test has 9 questions. The total mark for this paper is 48.
- The marks for **each** question are shown in brackets
  – *use this as a guide as to how much time to spend on each question*.

Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.
- This set of problem-solving questions is taken from Edexcel's original set of Specimen Assessment Materials, since replaced.

1. Pavel has a combination lock.

Pavel has to set each part of the lock to a digit between 0 and 9 inclusive.
One possible way to do this is shown in the diagram.

| 0 | 8 | 0 | 7 |
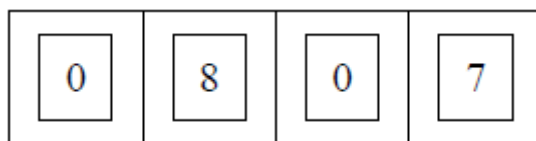
(*a*) How many different ways can Pavel do this?

(2)

Pavel decides that the 1st and 3rd digits will be odd numbers and that the 2nd and 4th digits will be even numbers greater than 0.

(*b*) How many different ways are possible now?

(2)

(Total for Question 1 is 4 marks)

2. **C** is the curve with equation $y = x^2 - 4x + 4$

L is the straight line with equation $y = 2x - 4$

L intersects **C** at two points, A and B.

Calculate the exact length of AB.

(Total for Question 2 is 6 marks)

3.   Here is a solid bar made of metal.

The bar is in the shape of a cuboid.
The height of the bar is h cm.
The base of the bar is a square of side d cm.
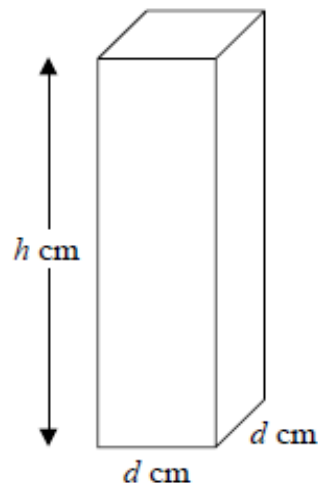
The mass of the bar is M kg.

$d = 8.3$ correct to 1 decimal place.
$M = 13.91$ correct to 2 decimal places.
$h = 84$ correct to the nearest whole number.

Find the value of the density of the metal to an appropriate degree of accuracy.
Give your answer in g/cm^3.

You must explain why your answer is to an appropriate degree of accuracy.

(Total for Question 3 is 5 marks)

4. (*a*) Expand and simplify $x(x + 1)(x - 1)$

(2)

In a list of three consecutive positive integers at least one of the numbers is even and one of the numbers is a multiple of 3.

n is a positive integer greater than 1.

(*b*) Prove that $n^3 - n$ is a multiple of 6 for all possible values of *n*.

(2)

$2^{61} - 1$ is a prime number.

(*c*) Explain why $2^{61} + 1$ is a multiple of 3.

(2)

(Total for Question 4 is 6 marks)

*5. The diagram shows triangle *ABC*.
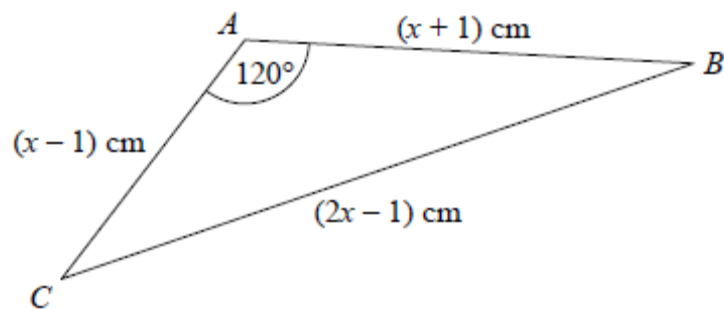
The area of triangle *ABC* is $k\sqrt{3}$ cm².

Find the exact value of k.

(Total for Question 5 is 7 marks)

6. Alfred studies animal populations on an island.

The size of an animal population at the start of 2014 was 2500.

The size of this animal population increases exponentially.

Alfred assumes that the rate of increase is 20% per year.

(*a*) Using his assumption, work out the size of this animal population at the start of 2009.

(3)

(*b*) Alfred's assumption is too high. Explain how your answer to part (a) is affected.

(1)

(Total for Question 6 is 4 marks)

7. A rectangular sheet of paper can be cut into two identical rectangular pieces in two different ways.
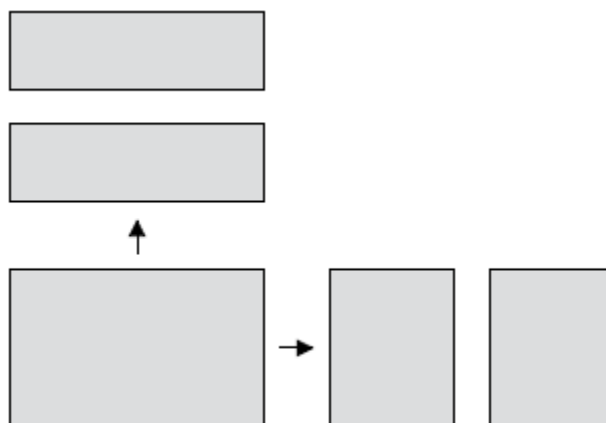
When the original sheet of paper is cut one way, the perimeter of each of the two pieces is 50 cm.

When the original sheet of paper is cut the other way, the perimeter of each of the two pieces is 64 cm.

What is the perimeter of the original sheet of paper?

(Total for Question 7 is 5 marks)

8. The quantity of heat, *H* calories, delivered by an electric current, *I* amps, acting for *t* seconds to heat an amount of water is given by the formula

$$H = atI^2 - b$$

where *a* and *b* are constants.

(*a*) Rearrange the formula to make *I* the subject.

(2)

The graph gives information about the variation in the temperature, in °C, of an amount of water that is allowed to cool from 80 °C.
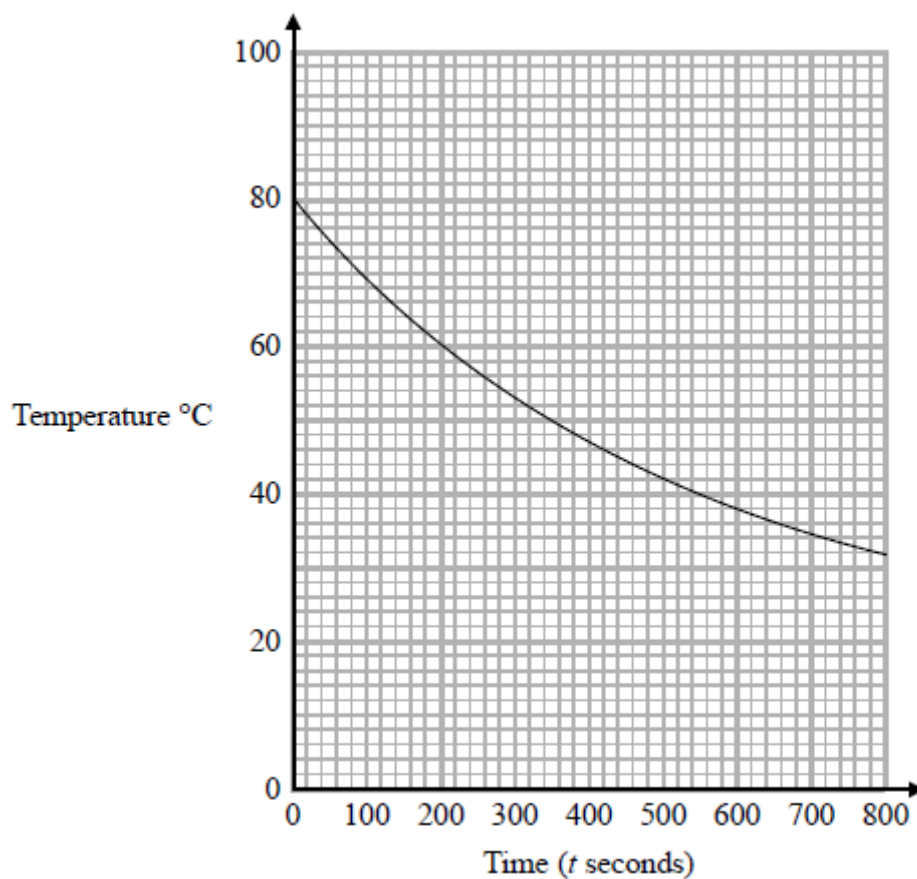
(*b*) (i) Work out the average rate of decrease of the temperature of the water
between $t = 0$ and $t = 800$.

The instantaneous rate of decrease of the temperature of the water at time T seconds
is equal to the average rate of decrease of the temperature of the water between $t = 0$
and $t = 800$.

(ii) Find an estimate for the value of T.
You must show how you got your answer.

(4)

(Total for Question 8 is 6 marks)

9.
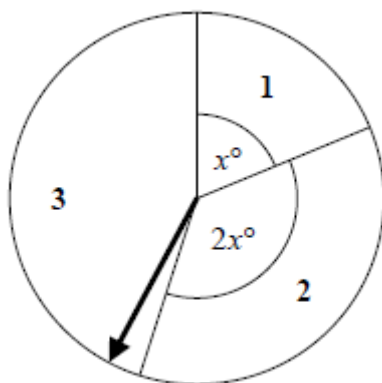
Here is a spinner.
When the arrow is spun once, a 1 or a 2 or a 3 can be scored.

Bill is going to spin the arrow twice.
He will work out his total score by adding the two scores he gets on the two spins.

The probability that he will get a total score of 4 is $\dfrac{16}{81}$

Assuming that the thickness of the three lines between the sectors may be ignored,

Work out the value of x.

<div align="right">

(Total for Question 9 is 5 marks)

</div>

BLANK PAGE

Question	Working	Answer	Mark	AO	Notes
1 (a)	$10 \times 10 \times 10 \times 10$	10000	M	1.3a	M1 $10 \times 10 \times 10 \times 10$
			A	1.3a	A1 cao
(b)	$5 \times 4 \times 5 \times 4$	400	M	1.3a	M1 $5 \times 4 \times 5 \times 4$
			A	1.3a	A1 cao
2	$2x - 4 = x^2 - 4x + 4$ $x^2 - 6x + 8 = 0$	$\sqrt{20}$	P	3.1b	P1 for a process to eliminate y, e.g. $2x - 4 = x^2 - 4x + 4$ followed by reduction to 3 term quadratic
	$(x - 4)(x - 2) = 0$		P	3.1b	P1 for factorisation or formula for a 3 term quadratic $= 0$
	$x = 4, \quad x = 2$		P	3.1b	P1 for a process to find the values of y
	When $x = 4$, $y = 4$		A	1.3b	A1 all 4 values ($x = 4$, $y = 4$, and $x = 2$, $y = 0$)
	When $x = 2$, $y = 0$		P	3.1a	P1 for a correct process to find the distance^2 or distance between the 2 points, e.g. ('4' − '2')2 + ('4' − '0')2
	$4 - 2 = 2$ $4 - 0 = 4$		A	1.3a	A1 $\sqrt{20}$
	$22 + 42$				

Question	Working	Answer	Mark	AO	Notes
3	$\dfrac{1000 \times 13..915}{8.25^2 \times 83.5} = 2.448$	2.4 g /cm^3	B	1.1	B1 for $83.5 \le h < 84.5$ or $8.25 \le d < 8.35$ (or correct bounds) or $13.905 \le M < 13.915$ (or correct bounds). Accept $h = 84.5$ or $d = 8.35$ or $M = 13.915$
			P	3.1c	P1 for correct process to find upper bound of D (= 2.4(48... or 0.0024(48...)) oe
	$\dfrac{1000 \times 13..905}{8.35^2 \times 84.5} = 2.360$		P	3.1c	P1 for correct process to find lower bound of D (= 2.3 (60... or 0.0023(6...)) oe
			P	2.4a	P1 for an explanation or a correct process to find D to an appropriate degree of accuracy
			A	1.3a	A1 2.4 g /cm^3
4 (a)		Shown	M	1.3a	M1 for $x(x^2 - 1)$ or $(x^2 + {}^x)({}^x - 1)$ oe
			A	1.3a	A1 cao
(b)		Shown	P	2.4b	P1 for explanation to show that $n^3 - n$ is the product of three consecutive positive integers, e.g. $n^3 - n = (n-1)n(n+1)$
			C	2.4b	C1 for a correct conclusion to the proof, e.g. at least one of these is even and one is a multiple of 3 so the product is a multiple of 6
(c)	$2^{61} - 1$ is prime so not a multiple of 3 2^{61} is not a multiple of 3 Hence $2^{61} + 1$ must be a multiple of 3	Shown	P	2.4a	P1 for recognising that $2^{61} - 1, 2^{61}$ and $2^{61} + 1$ are three consecutive positive integers
			C	2.4a	C1 for a convincing argument

Question	Working	Answer	Mark	AO	Notes
*5	$(2x-1)^2 =$ $(x+1)^2 + (x-1)^2 - 2(x+1)(x-1) \times$ $\cos 120°$	$\dfrac{15}{4}$	B	1.1	B1 for correct statement of cosine rule or $\dfrac{1}{2}ab\sin C$ or value of cos 120o or value of sin120°
	$4x^2 - 4x + 1 = x^2 + 2x + 1 + x^2 - 2x +$ $1 - 2(x^2 - 1) \times (-0.5)$		P	3.2	P1 for strategy to start to solve problem, e.g. $(2x-1)^2 = (x+1)^2 + (x-1)^2 - 2(x+1)(x-1) \times$ $\cos 120°$
	$x^2 - 4x = 0$				
	$x = 4$		P	3.2	P1 for strategy to reduce to a quadratic equation, e.g. $x^2 - 4x = 0$
	Area $= 0.5 \times 3 \times 5 \times \sin 120°$				
			M	1.3b	M1 for method to solve quadratic equation
			P	3.2	P1 for attempt to use $0.5ab \sin C$ with numeric or algebraic values substituted
			P	3.2	P1 for process to equate to $k\sqrt{3}$
			A	1.3b	A1 for $k = \dfrac{15}{4}$ oe
6 (a)	$2500 = P \times 1.20^5$	1005	P	3.1c	P1 for process to translate problem into algebraic form, e.g. $2500 = P \times 1.20^5$
	$P = 2500 \div 1.20^5 = 1004.69$		M	1.3a	M1 $P = 2500 \div 1.20^5$
			A	1.3a	A1 1005

Question	Working	Answer	Mark	AO	Notes
6 (b)		Correct explanation	C	3.5	C1 for an explanation eg the original population size will be greater
7	Let h and w be the dimensions of the original rectangle $h + 2w = 50$ $2h + w = 64$ $w = 12, \ h = 26$ Perimeter $= 2 \times 12 + 2 \times 26$	76 cm	P	3.2	P1 for correct process to set up equations, e.g. $\dfrac{h}{2} + \dfrac{h}{2} + w + w = 50$ and $\dfrac{w}{2} + \dfrac{w}{2} + h + h = 64$
			P	3.1d	P1 for correct process to find value of one variable
			P	3.1d	P1 for correct process to find value of other variable
			P	3.1d	P1 for correct process to find numerical value of perimeter, e.g. $2 \times ('12' + '26')$
			A	1.3b	A1 cao
8 (a)	$H = at\text{I}2 - b$ $\dfrac{H + b}{at} = I^2$	$I = \sqrt{\dfrac{H + b}{at}}$	M	1.3b	M1 $\dfrac{H + b}{at} = I^2$
			A	1.3b	A1 cao (accept ±)
(b)(i)	$\dfrac{80 - 32}{800}$	0.06°C/second	P	3.1a	P1 for process to use graph to find gradient, e.g. $\dfrac{80 - 32}{0 - 800}$
(ii)	Draw a tangent to the curve with a gradient of –0.06 (see diagram at the end)	350 seconds	A	1.3a	A1 accept –0.06°C/second

Question	Working	Answer	Mark	AO	Notes
			P	2.3a	P1 for process to interpret parallel lines on diagram
			A	1.3a	A1 340 – 360
9		40	P	3.1d	P1 for identifying probabilites, e.g. probability of '1' $= \dfrac{x}{360}$, probability of '2' $= \dfrac{2x}{360}$, probability of '3' $= 1 - \dfrac{x}{360}$
			P	3.1d	P1 for a correct process to set up a quadratic equation, e.g. $2 \times \dfrac{x}{360} \times \left(1 - \dfrac{3x}{360}\right) + \left(\dfrac{2x}{360}\right)^2 = \dfrac{16}{81}$
			P	3.1d	P1 for a correct process that leads to a 3-term quadratic, e.g. $2x^2 - 720x + 25600 = 0$
			M	1.3b	M1 for a correct method to solve the quadratic equation, e.g. $(2x - 80)(x - 320)$ $(=0)$
			P	3.3	P1 selection of $x = 40$ (from solutions $x = 40$ or $x = 320$)