

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress Descriptor
<b>1ai</b>	If a $T$ statistic is used as an estimator for a population parameter $\theta$	<b>B1</b>	1.2	6th Explain what is meant by an unbiased estimator
	Then $T$ is an unbiased estimator for $\theta$ when $E(T) = \theta$	<b>B1</b>	1.2	
		<b>(2)</b>		
<b>1aii</b>	bias = $E(T) - \theta$	<b>B1</b>	1.2	6th Explain what is meant by bias in an estimator
		<b>(1)</b>		
<b>1b</b>	$(\mu = \bar{x} =) \frac{2718}{75} = 36.24$	<b>M1</b>	1.1b	5th Understand how a sample statistic may be used to estimate a population parameter
	$(\sigma^2 = s^2 =) \frac{1}{74} \left( 98984 - \frac{2718^2}{75} \right) = 6.536\dots$	<b>M1</b> <b>A1</b>	1.1b 1.1b	
		<b>(3)</b>		
<b>(6 marks)</b>				
<b>Notes</b>				
<p><b>1ai B1:</b> for 'if a <math>T</math> statistic is used as an estimator for a population parameter <math>\theta</math>' o.e (may be seen in (i) or (ii))</p> <p><b>B1:</b> for <math>E(T) = \theta</math></p> <p><b>1aii B1:</b> for <math>E(T) - \theta</math></p> <p><b>1b M1:</b> for <math>\frac{2718}{75}</math></p> <p><b>M1:</b> for use of <math>\frac{1}{n-1} \left( \sum x^2 - \frac{\sum x^2}{n} \right)</math></p> <p><b>A1:</b> awrt 6.54</p>				

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress Descriptor
2a	$\bar{x} = \frac{38.8}{4} = 9.7$	M1	1.1b	6th Find a confidence interval for the mean of a normal distribution with known variance
	Z value = 1.96	B1	1.1 b	
	$9.7 \pm 1.96 \times \frac{0.36}{\sqrt{4}}$	M1	1.1b	
	(9.3472, 10.0528)	A1 A1	1.1b 1.1b	
		(5)		
2b	$2 \times 1.96 \times \frac{0.36}{\sqrt{4}} = 0.7056$	M1 A1	1.1b 1.1b	7th Explain the relationship between the width of a confidence interval and its size used
		(2)		
2c	$2 \times z_{\text{value}} \times \frac{0.36}{2} = 0.3$	M1	1.1b	7th Explain the relationship between the width of a confidence interval and its size used
	$z = 0.833$	A1	1.1b	
	$2\Phi(0.833) - 1 = 2(0.7967) - 1$	M1	2.1	
	$= 0.5934$ So confidence interval associated with width 0.3 is 59.34%	A1	1.1b	
		(4)		

<b>2d</b>	$2 \times 1.96 \times \frac{0.36}{\sqrt{n}} \leq 0.3$	<b>M1</b>	1.1b	7th Explain the relationship between the width of a confidence interval and the sample size
	$\sqrt{n} \dots 4.704$	<b>M1</b>	1.1b	
	$n \geq 22.127\dots$	<b>A1</b>	1.1b	
	So the sack would need to be weighed 23 times.	<b>A1</b>	2.2a	
		<b>(4)</b>		

**(15 marks)**

### Notes

**2a M1:** for  $\frac{38.8}{4}$

**B1:** for 1.96

**M1:** for use of  $\bar{x} \pm z_{\text{value}} \times \frac{s}{\sqrt{n}}$

**A1:** awrt 9.35

**A1:** awrt 10.1

**2b M1:** for use of  $2 \times z_{\text{value}} \times \frac{s}{\sqrt{n}}$

**A1:** for 0.7056

**2c M1:** for  $2 \times z_{\text{value}} \times \frac{s}{\sqrt{n}} = 0.3$

**A1:** awrt 0.83

**M1:** for either  $2\Phi(0.833) - 1$  or  $2(0.7967) - 1$

**A1:** awrt 59.3(%)

**2d M1:** for  $2 \times 1.96 \times \frac{0.36}{\sqrt{n}} = 0.3$

**M1:** for solving as far as  $\sqrt{n} \dots\dots$

**A1:**  $n \geq$  awrt 22.1

**A1:**  $n = 23$

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress Descriptor
<b>3a</b>	Z value = 1.96	<b>B1</b>	1.1b	6th
	$44.2 \pm 1.96 \times \frac{8}{\sqrt{25}}$	<b>M1</b>	1.1b	Find a confidence interval for the mean of a normal distribution with known variance
	(41.064, 47.336)	<b>A1</b> <b>A1</b>	1.1b 1.1b	
		<b>(4)</b>		
<b>3b</b>	$H_0 : \mu_1 = \mu_2$ $H_1 : \mu_1 > \mu_2$	<b>B1</b>	2.5	6th
	Z value = 1.6449	<b>B1</b>	1.1b	Carry out a hypothesis test for the difference between the means of two normal distributions with known variances
	$z = \frac{44.2 - 40.9}{\sqrt{\frac{64}{25} + \frac{64}{20}}} = 1.375$	<b>M1</b> <b>A1</b>	2.1 1.1b	
	Do not reject $H_0$ . There is not sufficient evidence for the mathematics teacher's conclusion that the mean for school B is less than that of school A	<b>A1</b>	2.2b	
		<b>(5)</b>		
<b>(9 marks)</b>				
<b>Notes</b>				
<b>3a</b>	<b>B1:</b> for 1.96			
	<b>M1:</b> for use of $\bar{x} \pm z_{\text{value}} \times \frac{s}{\sqrt{n}}$			
	<b>A1:</b> awrt 41.1			
	<b>A1:</b> awrt 47.3			
<b>3b</b>	<b>B1:</b> both hypotheses			
	<b>B1:</b> for 1.6449			
	<b>M1:</b> for use of $\frac{\bar{x}_A - \bar{x}_B}{\sqrt{\frac{\sigma_A^2}{n_A} + \frac{\sigma_B^2}{n_B}}}$			
	<b>A1:</b> for 1.375			
	<b>A1:</b> Drawing a correct inference, follow through their CV and test statistic			

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress Descriptor
4a	$H_0 : \mu_B = \mu_G$ $H_1 : \mu_B \neq \mu_G$	<b>B1</b>	2.5	6th  Carry out a hypothesis test for the difference between the means of two normal distributions with known variances
	$z = \frac{70 - 65}{\sqrt{\frac{14^2}{50} + \frac{14^2}{50}}} = 1.7857\dots$	<b>M1</b> <b>A1</b>	2.1 1.1b	
	Z value = 1.96	<b>B1</b>	1.1b	
	Do not reject $H_0$ . There is insufficient evidence to suggest that there is a difference between the mean scores of the boys and girls.	<b>A1</b>	2.2b	
		<b>(5)</b>		
4b	$H_0 : \mu_B = \mu_G$ $H_1 : \mu_B < \mu_G$	<b>B1</b>	2.5	6th  Carry out a hypothesis test for the difference between the means of two normal distributions with known variances
	$z = \frac{78 - 73}{\sqrt{\frac{7^2}{50} + \frac{7^2}{50}}} = 3.751\dots$	<b>M1</b> <b>A1</b>	2.1 1.1b	
	Z value = 1.6449	<b>B1</b>	1.1b	
	Reject $H_0$ . There is sufficient evidence to suggest that the mean mark for boys is less than the mean mark for girls.	<b>A1</b>	2.2b	
		<b>(5)</b>		
4c	Girls have improved more than boys or girls have performed better than boys after one year.	<b>B1</b>	2.2a	8th  Comment on claims made in the context of the question
		<b>(1)</b>		
				<b>(11 marks)</b>

**Notes**

**4a B1:** for both hypotheses

**M1:** for use of  $\frac{\bar{x}_G - \bar{x}_B}{\sqrt{\frac{\sigma_G^2}{n_G} + \frac{\sigma_B^2}{n_B}}}$

**A1:** awrt 1.79

**B1:** Z value = 1.96

**A1:** Drawing a correct inference, follow through their CV and test statistic

**4b B1:** for both hypotheses

**M1:** for use of  $\frac{\bar{x}_G - \bar{x}_B}{\sqrt{\frac{\sigma_G^2}{n_G} + \frac{\sigma_B^2}{n_B}}}$

**A1:** awrt 3.75

**B1:** Z value = 1.6449

**A1:** Drawing a correct inference, follow through their CV and test statistic

**4c B1:** Correct interpretation follow through parts **a** and **b**

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress Descriptor
5a	$\bar{x} = \frac{315}{70} = 4.5$	M1	1.1b	5th Understand how a sample statistic may be used to estimate a population parameter
	$s^2 = \frac{1}{69} \left( 1521 - \frac{315^2}{70} \right) = 1.5$	M1 A1	1.1b 1.1b	
		(3)		
5b	$H_0 : \mu_A = \mu_B \quad H_1 : \mu_A > \mu_B$	B1	2.5	7th Use large sample results to carry out the test with unknown population variances
	$z = \frac{4.5 - 4.04}{\sqrt{\frac{1.5}{70} + \frac{2.35}{60}}} = 1.8686\dots$	M1 A1	2.1 1.1b	
	Z value = 1.6449	B1	1.1b	
	Reject $H_0$ . There is sufficient evidence to suggest that the mean weight loss after the first month using training programme $A$ is greater than that using training programme $B$	A1	2.2b	
		(5)		
5c	The central limit theorem allows you to assume that the sample means of $A$ and $B$ follow a normal distribution.	B1	3.5b	7th Use large sample results to carry out the test with unknown population variances
		(1)		
				<b>(9 marks)</b>

## Notes

**5a M1:** for  $\frac{315}{70}$

**M1:** for use of  $\frac{1}{n-1} \left( \sum x^2 - \frac{\sum x^2}{n} \right)$

**A1:** for 1.5

**5b B1:** both hypotheses

**M1:** for use of  $\frac{\bar{x}_A - \bar{x}_B}{\sqrt{\frac{\sigma_A^2}{n_A} + \frac{\sigma_B^2}{n_B}}}$

**A1:** awrt 1.87

**B1:** Z value = 1.6449

**A1:** Drawing a correct inference, follow through their CV and test statistic

**5c B1:** for stating that the sample means of *A* and *B* follow a normal distribution