1.			41	28	42	31	36	32	29		
		numbers in the								are to be	;
	(a)	Calculate a statues.	lower bou	nd for the 1	number o	f crates tha	at will be	e needed t	to trans	port the	
											(2)
	(b)	Use the firs	t-fit bin pa	acking algo	rithm to ε	allocate the	e statues	to the cra	ites.		(3)
	(c)	Use the full	bin algori	thm to allo	cate the s	statues to t	he crates	S.			(2)
	(d)	Explain why		possible to	transport	the statue	s using f	ewer crat	es than		nber (2) tal 9 marks)
2.		32	45	17 23	38	28	16	9 1	2	10	
		numbers in th cut from roll				ths, in met	res, of te	en lengths	of fab	ric. They	/ are
	(a)	Calculate a	lower bou	nd for the 1	number o	f rolls nee	ded.				(2)
	(b)	Use the firs rolls of leng		acking algo	rithm to c	letermine	how thes	se ten leng	gths car	n be cut	from (4)
	(c)	Use full bin	s to find a	n optimal s	olution th	nat uses the	e minim	um numb	er of ro		(3) otal 9 marks)

**(2)** 

(Total 11 marks)

(c)

3.	29	52	73	87	74	47	38	61	41		
		numbers in ecorded ont		•		_			radio programmes. T ogrammes.	hey are to	
	(a)	Obtain a	lower bo	ound for	the nun	nber of ta	apes nee	ded to s	tore the nine program	nmes.	(2)
	(b)	Use the f	irst-fit b	in packi	ng algor	ithm to f	it the pr	ogramm	es onto the tapes.		(3)
	(c)	Use the f	irst-fit d	ecreasin	g bin pa	cking al	gorithm	to fit the	e programmes onto t	•	(3)
										(Total 8 m	arks)
4.		6	550 43	1 245	643	455 13	4 710	234	162 452		
	(a)		e sorted					_	order. Perform a Qu pass, indicating the		(5)
		numbers in ne metre ler		represer	nt the ler	igths, in	mm, of	some pi	eces of wood. The w	ood is sold	
	(b)						-		mine how these piecon should ignore wasta		
		Juling.)									<b>(4)</b>

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Determine whether your solution to part (b) is optimal. Give a reason for your answer.

5.	Nine pieces of wood are required to build a small cabinet. The lengths, in cm, of the pieces of
	wood are listed below.

20, 20, 20, 35, 40, 50, 60, 70, 75

Planks, one metre in length, can be purchased at a cost of £3 each.

(a) The first fit decreasing algorithm is used to determine how many of these planks are to be purchased to make this cabinet. Find the total cost and the amount of wood wasted.

**(5)** 

Planks of wood can also be bought in 1.5 m lengths, at a cost of £4 each. The cabinet can be built using a mixture of 1 m and 1.5 m planks.

(b) Find the minimum cost of making this cabinet. Justify your answer.

**(4)** 

(Total 9 marks)

**6.** 25 22 30 18 29 21 27 21

The list of numbers above is to be sorted into descending order.

- (a) (i) Perform the first pass of a bubble sort, giving the state of the list after each exchange.
  - (ii) Perform further passes, giving the state of the list after each pass, until the algorithm terminates.

**(5)** 

The numbers represent the lengths, in cm, of pieces to be cut from rods of length 50 cm.

- (b) (i) Show the result of applying the first fit decreasing bin packing algorithm to this situation.
  - (ii) Determine whether your solution to (b) (i) has used the minimum number of 50 cm rods.

**(4)** 

(Total 9 marks)

1. (a) e.g. total weight is 239, lower bound is  $\frac{239}{60} = 3.98$  so 4 bins. M1 A1 2

## **Note**

- 1M1: Any correct statement, must involve calculation
- 1A1: cao (accept 4 for both marks)
- (b) Bin 1 : 41 Bin 4 : 36 M1 A1 Bin 2 : 28 + 31 Bin 5 : 32 A1 3 Bin 3 : 42 Bin 6 : 29

#### Note

- 1M1: Bins 1 and 2 correct and at least 6 values put in bins
- 1A1: Bins 1, 2, 3 and 4 correct.
- 2A1: All correct

## Misread in (b) First Fit Decreasing

- Bin 1: 42 Bin 2: 41 Bin 3: 36 Bin 4: 32 28 Bin 5: 31 29 (Remove up to two A marks if earned so M1 max in (b) if first 4 bins correct.)
- (c) Full Bins: 28 + 32 31 + 29 M1 A1 2 The other 3 items (42, 41, 36) require 3 separate bins

### **Note**

- 1M1: Attempt to find two full bins and allocate at least 6 values 1A1: cao
- (d) There are 5 items over 30. No two of these 5 can be paired in a bin, so at least 5 bins will be required.

# **Note**

- 1B1: Correct argument may be imprecise or muddled (bod gets B1) 2B1: A good, clear, correct argument. (They have answered the question 'why?')
- 2. (a)  $\frac{230}{60} = 3.8\dot{3}$  so 4 needed M1 A1 2

### Note

- 1M1: Their 230 divided by 60, some evidence
  - of correct method 3.8 enough.
- 1A1: cso 4.

[9]

[9]

Bin 1: 32 17 9 (b) M1 A1 Bin 2: 45 12 **A**1 Bin 3: 23 28 **A**1 4 Bin 4: 38 16 Bin 5: 10 **Note** 1M1: Use of first fit. Probably 32, 45 and 17 correctly placed. 1A1: 32, 45, 17, 23, 38 and 28 placed correctly 2A1: 32, 45, 17, 23, 38, 28, 16, 9 placed correctly. 3A1: cao Special case for (b) misread using first fit decreasing. Give M1A1 (max) Bin 1: 45 12 Bin 2: 38 17 Bin 3: 32 28 Bin 4: 23 16 10 9 M1 for placing 45, 38, 32, 28 and 23 correctly A1 for cao. (c) e.g. Bin 1: 32 28 Bin 2: 38 12 10 M1 A1 Bin 3: 45 9 Bin 4: 23 17 16 **A**1 3 Note 1M1: Use of full bin – at least one full bin found and 5 numbers placed. 1A1: 2 full bins found Eg [32+28 and 38+12+10] [23+28+9 and 16+12+32] [32+28 and 23+16+12+9] [38+12+10 and 23+28+9] 2A1: A 4 bin solution found.

# D1 Algorithms - Bin packing

3. (a)  $\frac{502}{100} = 5.02$  so 6 tapes.

Ml

Al 2

1M1  $(502 \pm 40) \div 100$  (maybe implicit)

1A1: cao 6 tapes

(b) Bin 1: 29, 52

Bin 5: 47,38

Ml

Bin 2: 73 Bin 3: 87 Bin 6: 61 Bin 7: 41

Bin 4: 74

Al

Al 3

1M1 Bin 1 correct and at least 8 values put in bins

1A1: Condone one error, (e.g. extra, omission, 'balanced' swap).

2A1: All correct

(c) Binl: 87

Bin 4: 61,38

M1

Bin 2: 74

Bin 5: 52,47

**A**1

Bin 3: 73

Bin6: 41,29

Al

3

5

1M1 Bin 1 correct and at least 8 values put in bins

1A1: Condone one error, (e.g. extra, omission, 'balanced' swap).

2A1: All conect

[8]

**4.** (a) E.

E.g.							M1	A1 A1ft	A1ft A1
650	431	245	643	455	710	234	162	452	134
650	643	710	455	431	245	234	162	452	134
650	$\overline{710}$	643	455	431	245	452	234	(162)	134
710	650	643	455	431	452	245	234	162	134
710	650	643	455	452	431	245	234	162	134

(b) Bin 1 710 + 245

Bin 3 643 + 162 + 134

Bin 5 431

M1 A1

M1 A1ft

Bin 2 650 + 234

Bin 4 455 + 452

A1ft A1

2

4

2

(c) eg.

 $\frac{4116}{1000} = 4.116 \therefore 5 \text{ bins needed } \therefore \text{ optimal}$ 

[11]

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6

### D1 Algorithms - Bin packing

5. (a) Bin 1 – 75+20 Bin 2 – 70 +20 Bin 3 – 60+40 Bin 4 – 50+35 Bin 5 – 20

5 Planks needed: cost £15 A1
Wastage = 5+10+0+15+80 = 110cm A1 5

[9]

6.	(a)	(i)	le ft to right						or						right to le ft					
			25	22	30	18	29	21	27	21		25	22	30	18	29	21	27	21	M1
			25	30	22	18	29	21	27	21		25	22	30	18	29	27	28	21	
			25	30	22	29	18	21	27	21		25	22	30	29	18	27	21	21	
			25	30	22	29	21	18	27	21	_	25	30	22	29	18	27	21	21	
			25	30	22	29	21	27	18	21		30	25	22	29	18	27	21	21	A1 (pass)
		(ii)	25	30	22	29	21	27	21	18		30	29	25	22	27	18	21	21	
			30	25	29	22	27	21	21	18		30	29	27	25	22	21	18	21	
			30	29	25	27	22	21	21	18		30	29	27	25	22	21	21	18	
			30	29	27	25	22	21	21	18	-	30	29	27	25	22	21	21	18	
			30	29	27	25	22	21	21	18										

(ii)  $193 \div 50 = 3.86$ , : 4 rods needed, so minimum M1 A1 2

- 1. This was a good source of marks for well-prepared candidates with over 75% gaining at least 7 marks, though the final part challenged all but the most able.
  - Part (a) was almost always completed correctly.
  - Part (b) was often well done, although some used first fit decreasing and 29 was sometimes either omitted from the list or changed to 39.
  - Most candidates were able to complete part (c) correctly but a few only listed one full bin.
  - In part (d) many incorrectly stated that the full bin solution was optimal, others made some vague reference to the statues being too heavy, relatively few attempted a valid numerically based answer and managed to express it clearly.
- 2. This was often a good source of marks for candidates. Most were able to calculate the lower bound getting 3.8 and therefore 4 bins. Most candidates applied first fit correctly, although some candidates did not offer each item to each bin in turn, starting with bin 1 each time, so often the 9 was the first item to be misplaced. Some candidates wasted time by replacing each letter by a number, or explaining in lengthy detail the steps they took to place each item. Not all candidates realised that they should fill as many bins as possible when using full bin, most found one full bin, but only the best found two.
- 3. This proved an accessible first question and was well answered by many candidates. Some candidates probably spent too long on this question, drawing out very neat and accurate bar graphs in (b) and (c), where numbers in bins were perfectly acceptable. Most candidates calculated the lower bound correctly in part (a) although some attempted a full bin solution and others divided by 9, some having calculated 5.02 rounded down to 5. Apart from the usual omissions of data, part (b) was usually well answered, the most common slips being to swap the 38 and the 41, or to use the 52 to start off the second bin. First–Fit **increasing** was disappointingly often seen in part (c), but those who used the correct algorithm were usually successful with the only common error being misplacing the 38.
- 4. Some very good answers were seen to part (a), but many candidates produced disappointing attempts. Poor presentation and lack of concentration accounted for most errors in part (a); there was inconsistent choice of pivots, numbers that disappeared from the list, numbers that mutated into other numbers and, of course, numbers being reordered in the list. A large minority sorted the list into ascending order. A number of candidates are only selecting one pivot per pass, which rather defeats the object of a quick sort. Only a very few Bubble sorts were seen. Candidate would help themselves hugely by not fixing the position of the pivots until the line after they are selected, this would avoid the need to try to cram numbers into the everdecreasing space formed by their previously chosen pivots. Candidates could then use the whole width of the line each time. Part (b) was usually well done. Some used the first fit algorithm and many put 134 into bin 5 rather than bin 3. Part (c) was often well attempted with the majority of candidates giving a clear, arithmetical argument.

- 5. Many candidates scored full marks in part (a); however some candidates used the values in ascending order scoring zero. There was no need to use a formal sort to put the list in order. Many candidates gave the cost of the wasted wood rather than the cost of the five planks. In part (b) many candidates found an optimal solution, but many then went on to consider just the amount of wood wasted, rather than showing that the cost depended upon the value for money of each plank and therefore maximising the number of 1.5m lengths used.
- 6. Most candidates were able to complete the bubble sort correctly, although a number of shuttle sorts were seen from a few candidates. A number of candidates did not complete a final pass, (or stated that they had performed a final pass and found no further exchanges). The majority were able to complete the bin packing but a number were unable to show that they had used a minimum number of bins, once again the lower bound would have helped here.